SHIKSHA CLASSES, BHANDARA

Jee Paper 31 Jan 2024 Shift ll

Subject:- Chemistry, Physics, Mathematics

Time: 180 (in min)

Marks: 296

INSTRUCTIONS:-

Syllabus:-

Physics

- Single Correct Answer Type

(1) The measured value of the length of a simple pendulum is 20 cm with 2 mm accuracy. The time for 50 oscillations was measured to be 40 seconds with 1 second resolution. From these measurements, the accuracy in the measurement of acceleration due to gravity is N%. The value of N is:

(1) 4

(2) 8

(3) 6

(4) 5

(2) When unpolarized light is incident at an angle of 60° on a transparent medium from air. The reflected ray is completely polarized. The angle of refraction in the medium is

(1) 30^0

(2) 60^0

(3) 90^0

(4) 45^0

(3) An AC voltage $V = 20\sin 200\pi t$ is applied to a series LCR circuit which drives a current $I = 10\sin\left(200\pi t + \frac{\pi}{3}\right)$. The average power dissipated is:

(1) 21.6 W

(2) 200 W

(3) 173.2 W

(4) 50 W

(4) A uniform magnetic field of 2×10^{-3} T acts along positive Y-direction. A rectangular loop of sides 20 cm and 10 cm with current of 5 A is Y-Z plane. The current is in anticlockwise sense with reference to negative X axis. Magnitude and direction of the torque is :

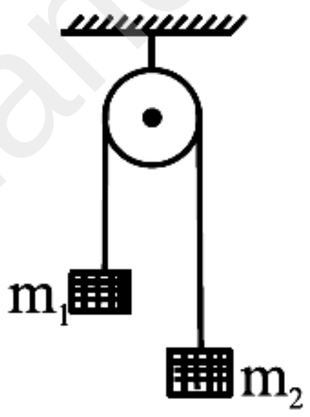
(1) 2×10^{-4} N – m along positive Z –direction

(2) 2×10^{-4} N – m along negative Z-direction

(3) 2×10^{-4} N – m along positive X-direction

(4) 2×10^{-4} N – m along positive Y-direction

(5) A light string passing over a smooth light fixed pulley connects two blocks of masses m_1 and m_2. If the acceleration of the system is g/8, then the ratio of masses is



(1) $\frac{9}{7}$

(2) $\frac{8}{1}$

(3) $\frac{4}{3}$

(4) $\frac{5}{3}$

(6) Given below are two statements:
Statement I: Electromagnetic waves carry energy as they travel through space and this energy is equally shared by the electric and magnetic fields.
Statement II: When electromagnetic waves strike a surface, a pressure is exerted on the surface.
In the light of the above statements, choose the most appropriate answer from the options given below:

(1) Statement I is incorrect but Statement II is correct

(2) Both Statement I and Statement II are correct.

(3) Both Statement I and Statement II are incorrect.

(4) Statement I is correct but Statement II is incorrect.

(7) The resistance per centimeter of a meter bridge wire is r, with X Ω resistance in left gap. Balancing length from left end is at 40 cm with 25 Ω resistance in right gap. Now the wire is replaced by another wire of 2r resistance per centimeter. The new balancing length for same settings will be at

(1) 20 cm

(2) 10 cm

(3) 80 cm

(4) 40 cm

(8) **A** gas mixture consists of 8 moles of argon and 6 moles of oxygen at temperature T. Neglecting all vibrational modes, the total internal energy of the system is

(1) 29 RT

(2) 20 RT

(3) 27 RT

(4) 21 RT

(9) The mass number of nucleus having radius equal to half of the radius of nucleus with mass number 192 is:

(1) 24

(2) 32

(3) 40

(4) 20

(10) A body of mass 2 kg begins to move under the action of a time dependent force given by $\vec{F} = \left(6t\,\hat{i} + 6t^2\,\hat{j}\right)N$. The power developed by the force at the time t is given by:

(1) $\left(6t^4 + 9t^5\right)W$

(2) $\left(3t^3 + 6t^5\right)W$

(3) $\left(9t^5 + 6t^3\right)W$

(4) $\left(9t^3 + 6t^5\right)W$

(11) A small spherical ball of radius r, falling through a viscous medium of negligible density has terminal velocity 'v'. Another ball of the same mass but of radius 2r, falling through the same viscous medium will have terminal velocity:

(1) $\frac{v}{2}$

(2) $\frac{v}{4}$

(3) 4v

(4) 2v

(12) The speed of sound in oxygen at S.T.P. will be approximately:

(Given, $R = 8.3\,JK^{-1}, \gamma = 1.4$)

(1) 315 m / s

(2) 333 m/s

(3) 341 m/s

(4) 325 m/s

(13) If two vectors $\vec{A}$ and $\vec{B}$ having equal magnitude R are inclined at an angle θ, then

(1) $\left|\vec{A} - \vec{B}\right| = \sqrt{2}\,R\sin\left(\frac{\theta}{2}\right)$

(2) $\left|\vec{A} + \vec{B}\right| = 2\,R\sin\left(\frac{\theta}{2}\right)$

(3) $\left|\vec{A} + \vec{B}\right| = 2\,R\cos\left(\frac{\theta}{2}\right)$

(4) $\left|\vec{A} - \vec{B}\right| = 2\,R\cos\left(\frac{\theta}{2}\right)$

(14) By what percentage will the illumination of the lamp decrease if the current drops by 20%?

(1) 46%

(2) 26%

(3) 36%

(4) 56%

(15) Force between two point charges q_1 and q_2 placed in vacuum at 'r' cm apart is F. Force between them when placed in a medium having dielectric K = 5 at 'r/5' cm apart will be:

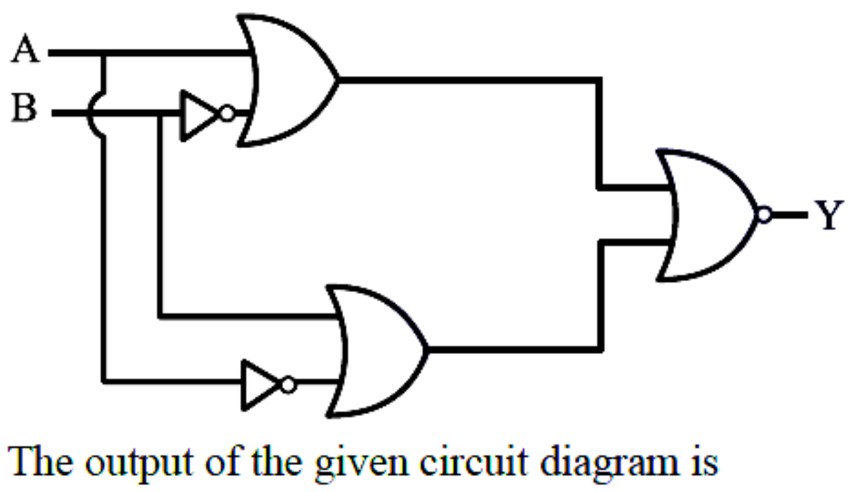
(1) F/25

(2) 5F

(3) F/5

(4) 25F

(16)



The output of the given circuit diagram is

(1)

A	B	Y
0	0	0
1	0	0
0	1	0
1	1	1

(2)

A	B	Y
0	0	0
1	0	1
0	1	1
1	1	0

(3)

A	B	Y
0	0	0
1	0	0
0	1	0
1	1	0

(4)

A	B	Y
0	0	0
1	0	0
0	1	1
1	1	0

(17) The mass of the moon is 1/144 times the mass of a planet and its diameter 1/16 times the diameter of a planet. If the escape velocity on the planet is v, the escape velocity on the moon will be:

(1) $\frac{v}{3}$

(2) $\frac{v}{4}$

(3) $\frac{v}{12}$

(4) $\frac{v}{6}$

(18) In a photoelectric effect experiment a light of frequency 1.5 times the threshold frequency is made to fall on the surface of photosensitive material. Now if the frequency is halved and intensity is doubled, the number of photo electrons emitted will be:

(1) Doubled

(2) Quadrupled

(3) Zero

(4) Halved

(19) Consider two physical quantities A and B related to each other as $E = \frac{B - x^2}{At}$ where E, x and t have dimensions of energy, length and time respectively. The dimension of AB is

(1) $L^{-2}M^{1}T^{0}$

(2) $L^{2}M^{-1}T^{1}$

(3) $L^{-2}M^{-1}T^{1}$

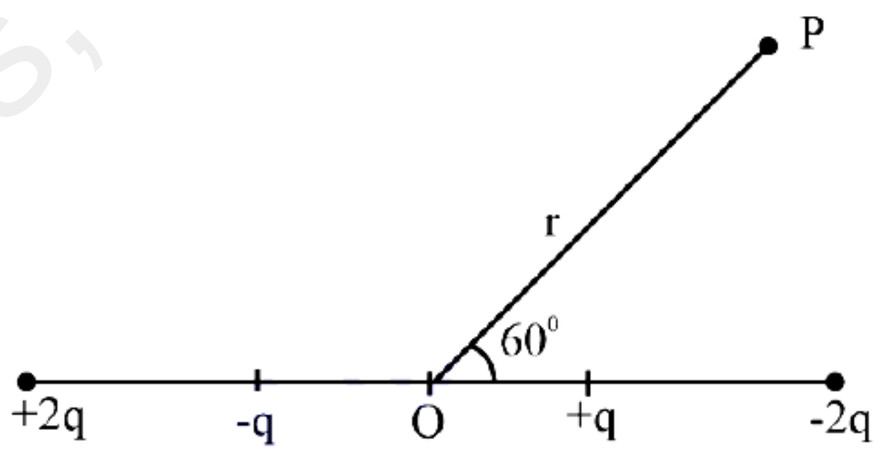
(4) $L^{0}M^{-1}T^{1}$

- Numerical value type

(20) The magnetic flux ϕ (in weber) linked with a closed circuit of resistance 8 Ω varies with time (in seconds) as $\phi = 5t^2 - 36t + 1$. The induced current in the circuit at $t = 2s$ is _____ A.

(21) Light from a point source in air falls on a convex curved surface of radius 20 cm and refractive index 1.5. If the source is located at 100 cm from the convex surface, the image will be formed at____ cm from the object.

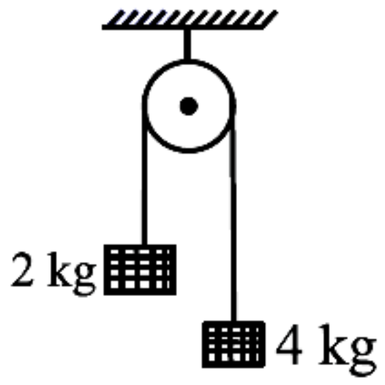
(22) The distance between charges +q and –q is $2l$ and between +2 q and -2 q is $4l$. The electrostatic potential at point P at a distance r from centre O is $-\alpha\left[\frac{ql}{r^2}\right] \times 10^9 V$, where the value of α is _____. (Use $\frac{1}{4\pi\varepsilon_0} = 9 \times 10^9\ Nm^2C^{-2}$)



(23) Two circular coils P and Q of 100 turns each have same radius of π cm. The currents in P and R are 1 A and 2 A respectively. P and Q are placed with their planes mutually perpendicular with their centers coincide. The resultant magnetic field induction at the center of the coils is $\sqrt{x}$ mT, where x =_____.

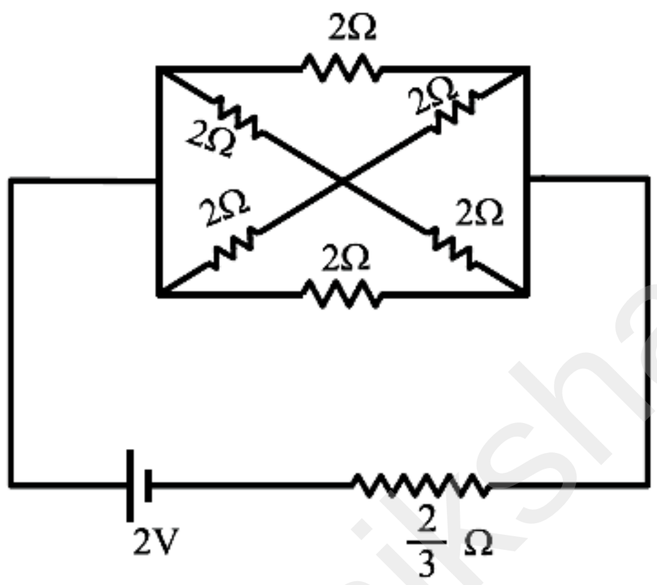
[Use $\mu_0 = 4\pi \times 10^{-7}\ TmA^{-1}$]

(24) Two blocks of mass 2 kg and 4 kg are connected by a metal wire going over a smooth pulley as shown in figure. The radius of wire is 4.0×10^{-5} m and Young's modulus of the metal is $2.0\times10^{11}\ N/m^2$. The longitudinal strain developed in the wire is $\frac{1}{\alpha\pi}$. The value of α is____. [Use $g=10\ m/s^2$)

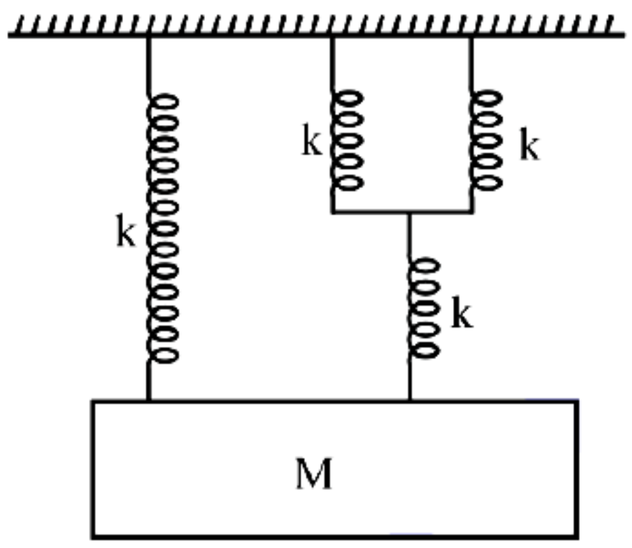


(25) Two identical spheres each of mass 2 kg and radius 50 cm are fixed at the ends of a light rod so that the separation between the centers is 150 cm. Then, moment of inertia of the system about an axis perpendicular to the rod and passing through its middle point is $\frac{x}{20}kg\ m^2$, where the value of x is ____.

(26) In the following circuit, the battery has an emf of 2 V and an internal resistance of $\frac{2}{3}\Omega$. The power consumption in the entire circuit is _____ W.



(27) The time period of simple harmonic motion of mass M in the given figure is $\pi\sqrt{\frac{\alpha M}{5K}}$, where the value of α is _____.



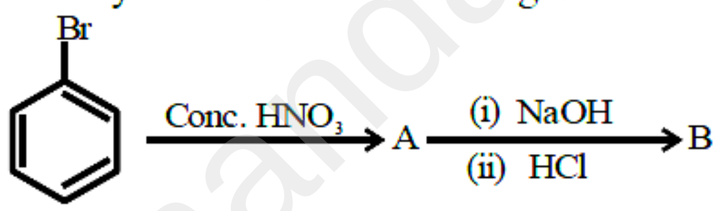
(28) A nucleus has mass number A_1 and volume V_1. Another nucleus has mass number A_2 and volume V_2. If relation between mass number is $A_2=4A_1$, then $\frac{V_2}{V_1}=$_____.

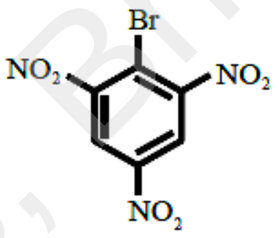
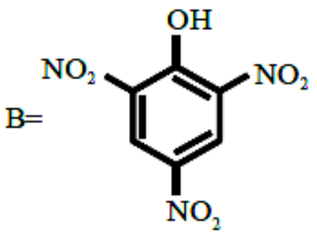
(29) A body of mass 'm' is projected with a speed 'u' making an angle of 45° with the ground. The angular momentum of the body about the point of projection, at the highest point is expressed as $\frac{\sqrt{2}\ mu^3}{Xg}$. The value of 'X' is_____.

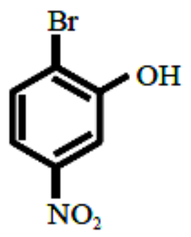
Chemistry

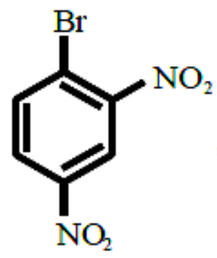
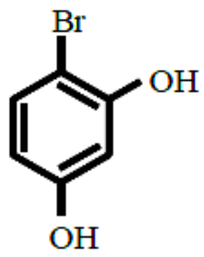
- Single Correct Answer Type

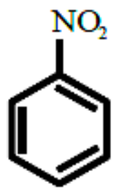
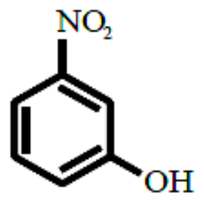
(30) Identify A and B in the following reaction sequence.



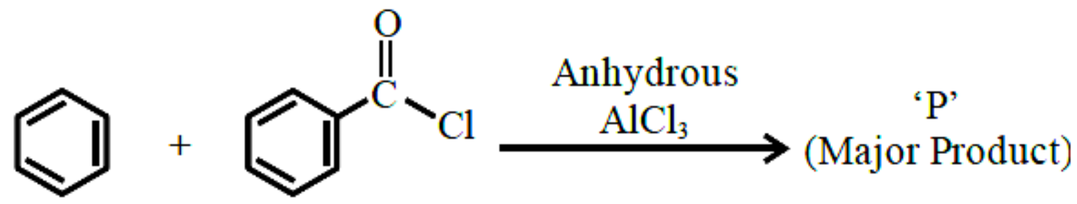
(1) A=  , B= 

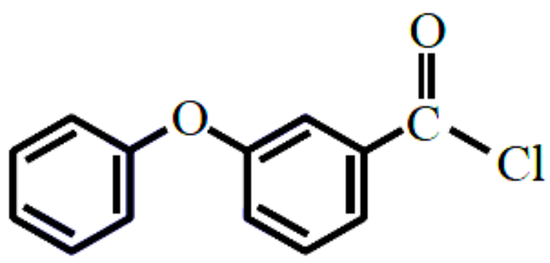
(2) A=  , B= 

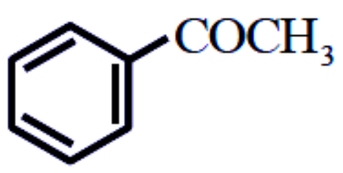
(3) A=  , B= 

(4) A=  , B= 

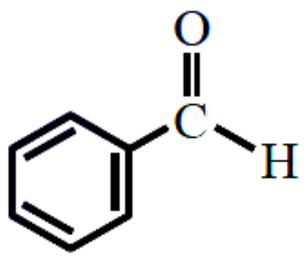
(31) Identify major product 'P' formed in the following reaction.



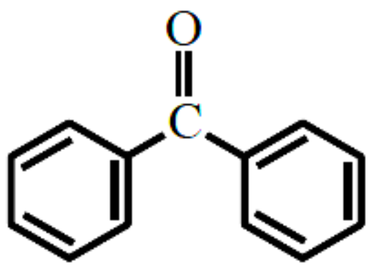
(1) 

(2) 

(3)

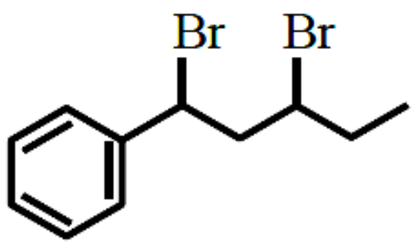


(4)



(32) Identify structure of 2,3-dibromo-1-phenylpentane.

(1)



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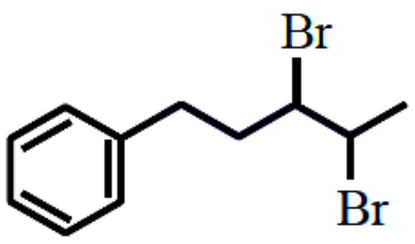

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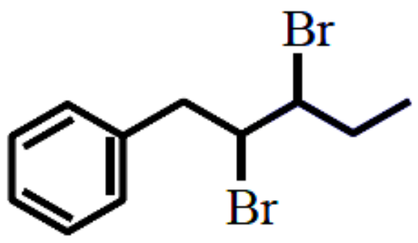

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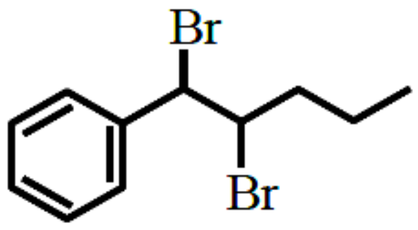


(33) Given below are two statements :

Statement I: Aniline reacts with con. H_2SO_4 followed by heating at 453-473 K gives p-aminobenzene sulphonic acid, which gives blood red colour in the 'Lassaigne's test'.

Statement II: In Friedel - Craft's alkylation and acylation reactions, aniline forms salt with the $AlCl_3$ catalyst. Due to this, nitrogen of aniline aquires a positive charge and acts as deactivating group.

In the light of the above statements, choose the ***correct answer*** from the options given below :

(1) Statement I is false but statement II is true

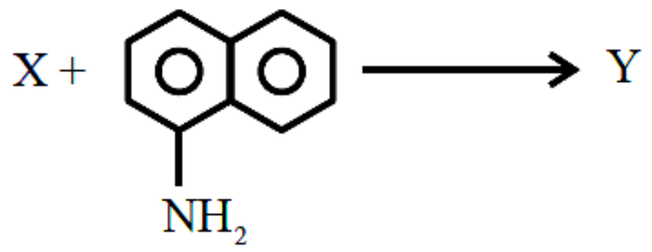
(2) Both statement I and statement II are false

(3) Statement I is true but statement II is false

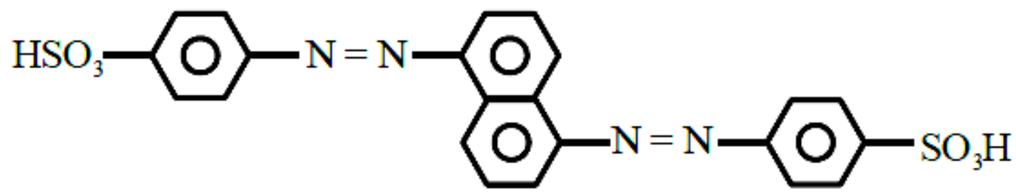
(4) Both statement I and statement II are true

(34) The azo-dye (Y) formed in the following reactions

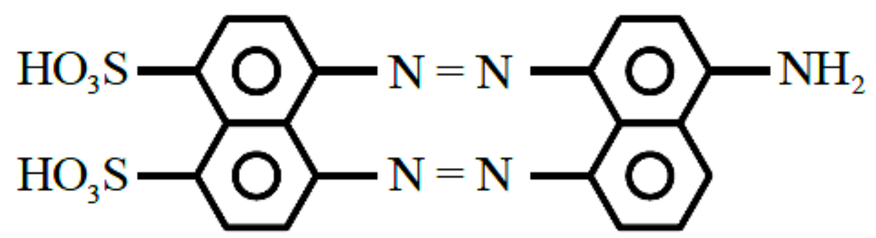
is Sulphanilic acid + $NaNO_2$ + $CH_3COOH \rightarrow X$



(1)



(2)



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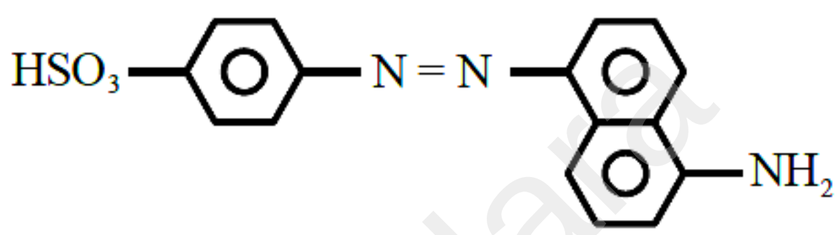

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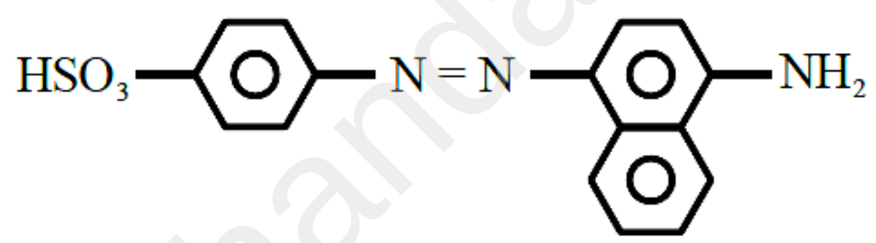
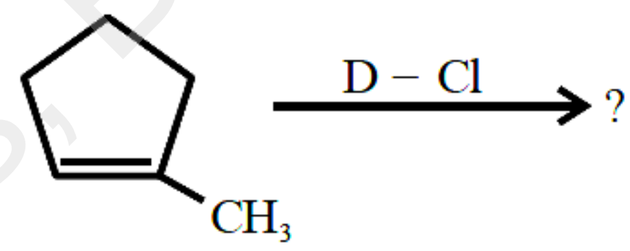
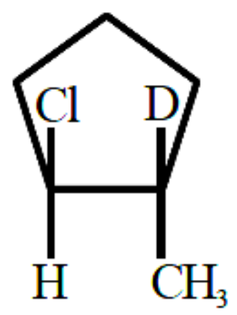


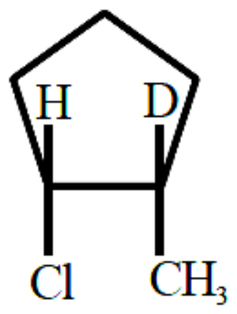
(35) Major product of the following reaction is –



(1)



(2)



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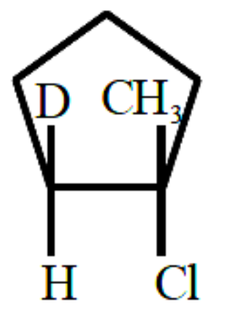

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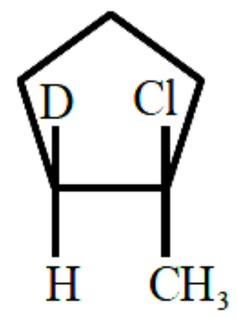


(36) $A_{(g)} \rightleftharpoons B_{(g)} + \frac{C}{2}(g)$ The correct relationship between K_P, α and equilibrium pressure P is

(1) $K_P = \frac{\alpha^{1/2} P^{1/2}}{(2+\alpha)^{1/2}}$

(2) $K_P = \frac{\alpha^{3/2} P^{1/2}}{(2+\alpha)^{1/2}(1-\alpha)}$

(3) $K_P = \frac{\alpha^{1/2} P^{3/2}}{(2+\alpha)^{3/2}}$

(4) $K_P = \frac{\alpha^{1/2} P^{1/2}}{(2+\alpha)^{3/2}}$

(37) Match List I with List II

	LIST – I (Complex ion)		LIST – II (Electronic Configuration
A.	$[Cr(H_2O)_6]^{3+}$	I.	$t_{2g}^2 e_g^0$
B.	$[Fe(H_2O)_6]^{3+}$	II.	$t_{2g}^3 e_g^0$
C.	$[Ni(H_2O)_6]^{2+}$	III.	$t_{2g}^3 e_g^2$
D.	$[V(H_2O)_6]^{3+}$	IV.	$t_{2g}^6 e_g^2$

Choose the correct answer from the options given below :

(1) A-III, B-II, C-IV, D-I

(2) A-IV, B-I, C-II, D-III

(3) A-IV, B-III, C-I, D-II

(4) A-II, B-III, C-IV, D-I

(38) Select the option with correct property -

(1) $[Ni(CO)_4]$ and $[NiCl_4]^{2-}$ both diamagnetic

(2) $[Ni(CO)_4]$ and $[NiCl_4]^{2-}$ both paramagnetic

(3) $[NiCl_4]^{2-}$ diamagnetic, $[Ni(CO)_4]$ paramagnetic

(4) $[Ni(CO)_4]$ diamagnetic, $[NiCl_4]^{2-}$ paramagnetic

(39) Given below are two statements :

Statement I: S_8 solid undergoes disproportionation reaction under alkaline conditions to form S^{2-} and $S_2O_3^{2-}$

Statement II: ClO_4^- can undergo disproportionation reaction under acidic condition.

In the light of the above statements, choose the ***most appropriate answer*** from the options given below :

(1) Statement I is correct but statement II is incorrect.

(2) Statement I is incorrect but statement II is correct

(3) Both statement I and statement II are incorrect

(4) Both statement I and statement II are correct

(40) A sample of $CaCO_3$ and $MgCO_3$ weighed 2.21 g is ignited to constant weight of 1.152 g. The composition of mixture is :

(Given molar mass in g mol^{-1}

$CaCO_3$: 100, $MgCO_3$: 84)

(1) 1.187 g $CaCO_3$ + 1.023 g $MgCO_3$

(2) 1.023 g $CaCO_3$ + 1.023 g $MgCO_3$

(3) 1.187 g $CaCO_3$ + 1.187 g $MgCO_3$

(4) 1.023 g $CaCO_3$ + 1.187 g $MgCO_3$

(41) The fragrance of flowers is due to the presence of some steam volatile organic compounds called essential oils. These are generally insoluble in water at room temperature but are miscible with water vapour in vapour phase. A suitable method for the extraction of these oils from the flowers is -

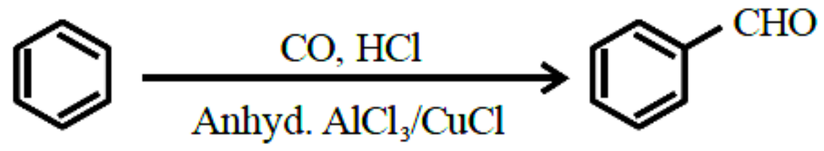
(1) crystallisation

(2) distillation under reduced pressure

(3) distillation

(4) steam distillation

(42) Identify the name reaction.



(1) Stephen reaction

(2) Etard reaction

(3) Gatterman-koch reaction

(4) Rosenmund reduction

(43) Choose the correct statements from the following

A. All group 16 elements form oxides of general formula EO_2 and EO_3 where E = S, Se, Te and Po. Both the types of oxides are acidic in nature.

B. TeO_2 is an oxidising agent while SO_2 is reducing in nature.

C. The reducing property decreases from H_2S to H_2Te down the group.

D. The ozone molecule contains five lone pairs of electrons.

Choose the correct answer from the options given below:

(1) A and D only

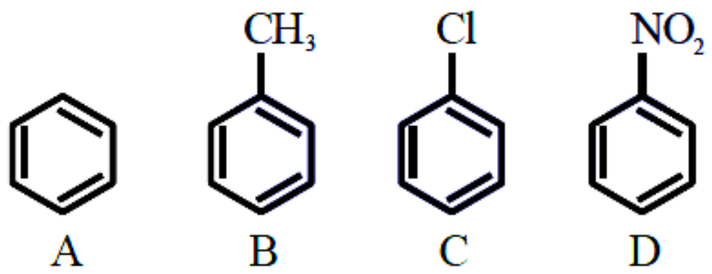
(2) B and C only

(3) C and D only

(4) A and B only

(44) The correct order of reactivity in electrophilic substitution reaction of the following compounds

is :



(1) $B > C > A > D$

(2) $D > C > B > A$

(3) $A > B > C > D$

(4) $B > A > C > D$

(45) The four quantum numbers for the electron in the outer most orbital of potassium (atomic no. 19) are

(1) $n = 4,\ l = 2,\ m = -1,\ s = +\frac{1}{2}$

(2) $n = 4,\ l = 0,\ m = 0,\ s = +\frac{1}{2}$

(3) $n = 3,\ l = 0,\ m = 1,\ s = +\frac{1}{2}$

(4) $n = 2,\ l = 0,\ m = 0,\ s = +\frac{1}{2}$

(46) Consider the following elements.

Group ↓ A'B' → Period
C'D'

Which of the following is/are true about A', B', C' and D' ?

A. Order of atomic radii: $B' < A' < D' < C'$

B. Order of metallic character : $B' < A' < D' < C'$

C. Size of the element : $D' < C' < B' < A'$

D. Order of ionic radii : $B'^{+} < A'^{+} < D'^{+} < C'^{+}$

Choose the correct answer from the options given below :

(1) A only

(2) A, B and D only

(3) A and B only

(4) B, C and D only

(47) Which of the following is least ionic ?

(1) $BaCl_2$

(2) AgCl

(3) KCl

(4) $CoCl_2$

(48) Choose the correct statements from the following

A. Mn_2O_7 is an oil at room temperature

B. V_2O_4 reacts with acid to give VO_2^{2+}

C. CrO is a basic oxide

D. V_2O_5 does not react with acid

Choose the correct answer from the options given below :

(1) A, B and D only

(2) A and C only

(3) A, B and C only

(4) B and C only

(49) Given below are two statements :

Statement I: Group 13 trivalent halides get easily hydrolyzed by water due to their covalent nature.

Statement II: $AlCl_3$ upon hydrolysis in acidified aqueous solution forms octahedral $\left[Al(H_2O)_6\right]^{3+}$ ion.

In the light of the above statements, choose the ***correct answer*** from the options given below :

(1) Statement I is true but statement II is false

(2) Statement I is false but statement II is true

(3) Both statement I and statement II are false

(4) Both statement I and statement II are true

- Numerical value type

(50) Number of moles of H^+ ions required by 1 mole of MnO_4^- to oxidise oxalate ion to CO_2 is ____.

(51) A diatomic molecule has a dipole moment of 1.2 D. If the bond distance is 1Å , then fractional charge on each atom is _____ $\times 10^{-1}$ esu .

(Given $1\,D = 10^{-18}$ esu cm)

(52) Number of isomeric products formed by mono-chlorination of 2-methylbutane in presence of sunlight is _____.

(53) $r = k[A]$ for a reaction, 50% of A is decomposed in 120 minutes. The time taken for 90% decomposition of A is _____ minutes.

(54) The molarity of 1L orthophosphoric acid (H_3PO_4) having 70% purity by weight (specific gravity $1.54\ g\ cm^{-3}$) is _____M.

(Molar mass of $H_3PO_4 = 98\ g\ mol^{-1}$)

(55) A compound (x) with molar mass $108\ g\ mol^{-1}$ undergoes acetylation to give product with molar mass $192\ g\ mol^{-1}$. The number of amino groups in the compound (x) is _____.

(56) If 5 moles of an ideal gas expands from 10 L to a volume of 100 L at 300 K under isothermal and reversible condition then work, w, is $-x$ J. The value of x is _____.

(Given $R = 8.314\ J\ K^{-1}mol^{-1}$)

(57) The values of conductivity of some materials at 298.15 K in Sm^{-1} are 2.1×10^{3}, $1.0\times10^{-16}, 1.2\times10, 3.91, 1.5\times10^{-2}$, $1\times10^{-7}, 1.0\times10^{3}$. The number of conductors among the materials is _____.

(58) In the reaction of potassium dichromate, potassium chloride and sulfuric acid (conc.), the oxidation state of the chromium in the product is (+)_____.

(59) From the vitamins A, B_1, B_6, B_{12}, C, D, E and K, the number vitamins that can be stored in our body is _____.

Mathematics

- Single Correct Answer Type

(60) Let a variable line passing through the centre of the circle $x^2 + y^2 - 16x - 4y = 0$, meet the positive co-ordinate axes at the point A and B. Then the minimum value of OA + OB, where O is the origin, is equal to

(1) 12
(2) 18
(3) 20
(4) 24

(61) Let (α,β,γ) be mirror image of the point (2, 3, 5) in the line $\frac{x-1}{2}=\frac{y-2}{3}=\frac{z-3}{4}$.

Then $2\alpha+3\beta+4\gamma$ is equal to

(1) 32
(2) 33
(3) 31
(4) 34

(62) The temperature T(t) of a body at time t = 0 is 160° F and it decreases continuously as per the differential equation $\frac{dT}{dt}=-K(T-80)$, where K is positive constant. If $T(15) = 120°F$, then T(45) is equal to

(1) 85° F
(2) 95° F
(3) 90° F
(4) 80° F

(63) Let $f:\to R\to(0,\infty)$ be strictly increasing function such that $\lim\limits_{x\to\infty}\frac{f(7x)}{f(x)}=1$. Then, the value of $\lim\limits_{x\to\infty}\left[\frac{f(5x)}{f(x)}-1\right]$ is equal to

(1) 4
(2) 0
(3) 7/5
(4) 1

(64) Let A (a, b), B(3, 4) and (–6, –8) respectively denote the centroid, circumcentre and orthocentre of a triangle. Then, the distance of the point P(2a + 3, 7b + 5) from the line 2x + 3y – 4 = 0 measured parallel to the line x – 2y – 1 = 0 is

(1) $\frac{15\sqrt{5}}{7}$
(2) $\frac{17\sqrt{5}}{6}$
(3) $\frac{17\sqrt{5}}{7}$
(4) $\frac{\sqrt{5}}{17}$

(65) Let $f,g:(0,\infty)\to R$ be two functions defined by $f(x)=\int_{-x}^{x}\left(|t|-t^2\right)e^{-t^2}dt$ and $g(x)=\int_{0}^{x^2}t^{1/2}e^{-t}dt$.

Then the value of $\left(f\left(\sqrt{\log_e 9}\right)+g\left(\sqrt{\log_e 9}\right)\right)$ is equal to

(1) 6
(2) 9
(3) 8
(4) 10

(66) Let 2^{nd}, 8^{th} and 44^{th}, terms of a non-constant A.P. be respectively the 1^{st}, 2^{nd} and 3^{rd} terms of G.P. If the first term of A.P. is 1 then the sum of first 20 terms is equal to-

(1) 980
(2) 960
(3) 990
(4) 970

(67) Let the mean and the variance of 6 observation a, b, 68, 44, 48, 60 be 55 and 194, respectively if $a > b$, then $a + 3b$ is

(1) 200
(2) 190
(3) 180
(4) 210

(68) The number of ways in which 21 identical apples can be distributed among three children such that each child gets at least 2 apples, is

(1) 406
(2) 130
(3) 142
(4) 136

(69) Let P be a parabola with vertex (2, 3) and directrix $2x + y = 6$. Let an ellipse $E: \frac{x^2}{a^2} + \frac{y^2}{b^2} = 1, a > b$ of eccentricity $\frac{1}{\sqrt{2}}$ pass through the focus of the parabola P. Then the square of the length of the latus rectum of E, is

(1) $\frac{385}{8}$
(2) $\frac{347}{8}$
(3) $\frac{512}{25}$
(4) $\frac{656}{25}$

(70) The number of solutions, of the equation $e^{\sin x} - 2e^{-\sin x} = 2$ is

(1) 2
(2) more than 2
(3) 1
(4) 0

(71) Consider the function $f:(0,\infty) \to R$ defined by $f(x) = e^{-|\log_e x|}$. If m and n be respectively the number of points at which f is not continuous and f is not differentiable, then m + n is

(1) 0
(2) 3
(3) 1
(4) 2

(72) The area of the region enclosed by the parabola $y = 4x - x^2$ and $3y = (x-4)^2$ is equal to

(1) $\frac{32}{9}$
(2) 4
(3) 6
(4) $\frac{14}{3}$

(73) Let z_1 and z_2 be two complex number such that $z_1 + z_2 = 5$ and $z_1^3 + z_2^3 = 20 + 15i$. Then $\left|z_1^4 + z_2^4\right|$ equals-

(1) $30\sqrt{3}$
(2) 75
(3) $15\sqrt{15}$
(4) $25\sqrt{3}$

(74) If for some m, n; ${}^6C_m + 2\left({}^6C_{m+1}\right) + {}^6C_{m+2} > {}^8C_3$ and ${}^{n-1}P_3 : {}^nP_4 = 1:8$, then ${}^nP_{m+1} + {}^{n+1}C_m$ is equal to

(1) 380
(2) 376
(3) 384
(4) 372

(75) Let A be a 3×3 real matrix such that

$$A\begin{pmatrix}1\\0\\1\end{pmatrix} = 2\begin{pmatrix}1\\0\\1\end{pmatrix}, A\begin{pmatrix}-1\\0\\1\end{pmatrix} = 4\begin{pmatrix}-1\\0\\1\end{pmatrix}, A\begin{pmatrix}0\\1\\0\end{pmatrix} = 2\begin{pmatrix}0\\1\\0\end{pmatrix}.$$

Then, the system $(A-3I)\begin{pmatrix}x\\y\\z\end{pmatrix} = \begin{pmatrix}1\\2\\3\end{pmatrix}$ has

(1) unique solution
(2) exactly two solutions
(3) no solution
(4) infinitely many solutions

(76) If the function $f:(-\infty,-1]\to(a,b]$ defined by $f(x)=e^{x^3-3x+1}$ is one-one and onto, then the distance of the point P(2b + 4, a + 2) from the line $x+e^{-3}y=4$ is :

(1) $2\sqrt{1+e^6}$

(2) $4\sqrt{1+e^6}$

(3) $3\sqrt{1+e^6}$

(4) $\sqrt{1+e^6}$

(77) A coin is based so that a head is twice as likely to occur as a tail. If the coin is tossed 3 times, then the probability of getting two tails and one head is-

(1) $\frac{2}{9}$

(2) $\frac{1}{9}$

(3) $\frac{2}{27}$

(4) $\frac{1}{27}$

(78) If $a=\sin^{-1}(\sin(5))$ and $b=\cos^{-1}(\cos(5))$, then a^2+b^2 is equal to

(1) $4\pi^2+25$

(2) $8\pi^2-40\pi+50$

(3) $4\pi^2-20\pi+50$

(4) 25

(79) The shortest distance between lines L_1 and L_2, where $L_1:\frac{x-1}{2}=\frac{y+1}{-3}=\frac{z+4}{2}$ and L_2 is the line passing through the points $A(-4,4,3).B(-1,6,3)$ and perpendicular to the line $\frac{x-3}{-2}=\frac{y}{3}=\frac{z-1}{1}$, is

(1) $\frac{121}{\sqrt{221}}$

(2) $\frac{24}{\sqrt{117}}$

(3) $\frac{141}{\sqrt{221}}$

(4) $\frac{42}{\sqrt{117}}$

- Numerical value type

(80) Let A = {1, 2, 3, ...100}. Let R be a relation on A defined by (x, y) $\in$ R if and only if 2x = 3y. Let R_1 be a symmetric relation on A such that $R\subset R_1$ and the number of elements in R_1 is n. Then, the minimum value of n is _____.

(81) A line passes through A(4, –6, –2) and B(16, –2,4). The point P(a, b, c) where a, b, c are non-negative integers, on the line AB lies at a distance of 21 units, from the point A. The distance between the points P(a, b, c) and Q(4, –12, 3) is equal to ____.

(82) Let a, b, c be the length of three sides of a triangle satisfying the condition $(a^2+b^2)x^2-2b(a+c)x+(b^2+c^2)=0$. If the set of all possible values of x is the interval (α,β), then $12(\alpha^2+\beta^2)$ is equal to _____.

(83) Let the coefficient of x^r in the expansion of

$$(x+3)^{n-1}+(x+3)^{n-2}(x+2)+(x+3)^{n-3}(x+2)^2+.....+(x+2)^{n-1}$$

be α_r. If $\sum_{r=0}^{n}\alpha_r=\beta^n-\gamma^n,\beta,\gamma\in N$, then the value of $\beta^2+\gamma^2$ equals _____.

(84) $\left|\frac{120}{\pi^3}\int_0^{\pi}\frac{x^2\sin x\cos x}{\sin^4x+\cos^4x}dx\right|$ is equal to _____.

(85) Let $\vec{a}=3\hat{i}+2\hat{j}+\hat{k},\vec{b}=2\hat{i}-\hat{j}+3\hat{k}$ and $\vec{c}$ be a vector such that $(\vec{a}+\vec{b})\times\vec{c}=2(\vec{a}\times\vec{b})+24\hat{j}-6\hat{k}$ and $(\vec{a}-\vec{b}+\hat{i}).\vec{c}=-3$. Then $|\vec{c}|^2$ is equal to _____.

(86) Let A be a 3×3 matrix and det (A) = 2. If

$$n=\det\left(\underbrace{adj(adj(.....(adjA)))}_{\text{2024-times}}\right)$$

Then the remainder when n is divided by 9 is equal to _____.

(87) Let A(–2, –1), B(1, 0), $C(\alpha,\beta)$ and $D(\gamma,\delta)$ be the vertices of a parallelogram ABCD. If the point C lies on $2x - y = 5$ and the point D lies on $3x - 2y = 6$, then the value of $|\alpha+\beta+\gamma+\delta|$ is equal to _____.

(88) If $\lim\limits_{x\to0}\dfrac{ax^2e^x - b\log_e(1+x)+cxe^{-x}}{x^2\sin x}=1,$

then $16(a^2+b^2+c^2)$ is equal to _____.

(89) Let $y = y(x)$ be the solution of the differential equation

$$\sec^2 x\,dx+\left(e^{2y}\tan^2 x+\tan x\right)dy=0,$$

$0<x<\dfrac{\pi}{2}, y\left(\dfrac{\pi}{4}\right)=0$. If $y\left(\dfrac{\pi}{6}\right)=\alpha,$

Then $e^{8\alpha}$ is equal to _____.

Answer Key

Physics

1 --- 3	2 --- 1	3 --- 4	4 --- 2	5 --- 1	6 --- 2	7 --- 4	8 --- 3	9 --- 1	10 --- 4	11 --- 1	12 --- 1	13 --- 3	14 --- 3	15 --- 2
16 --- 3	17 --- 1	18 --- 3	19 --- 2	20 --- 2.0	21 --- 200.0	22 --- 27.0	23 --- 20.0	24 --- 12.0	25 --- 53.0	26 --- 3.0	27 --- 12.0	28 --- 4.0	29 --- 8.0	

Chemistry

30 --- 1	31 --- 4	32 --- 3	33 --- 4	34 --- 4	35 --- 3	36 --- 2	37 --- 4	38 --- 4	39 --- 1	40 --- 1	41 --- 4	42 --- 3	43 --- 4	44 --- 4
45 --- 2	46 --- 2	47 --- 2	48 --- 2	49 --- 4	50 --- 8.0	51 --- 0.0	52 --- 6.0	53 --- 399.0	54 --- 11.0	55 --- 2.0	56 --- 28721.0	57 --- 4.0	58 --- 11.0	59 --- 5.0

Mathematics

60 --- 2	61 --- 2	62 --- 3	63 --- 2	64 --- 3	65 --- 3	66 --- 4	67 --- 3	68 --- 4	69 --- 4	70 --- 4	71 --- 3	72 --- 3	73 --- 2	74 --- 4
75 --- 1	76 --- 1	77 --- 1	78 --- 2	79 --- 3	80 --- 66.0	81 --- 22.0	82 --- 36.0	83 --- 25.0	84 --- 15.0	85 --- 38.0	86 --- 7.0	87 --- 32.0	88 --- 81.0	89 --- 9.0